





























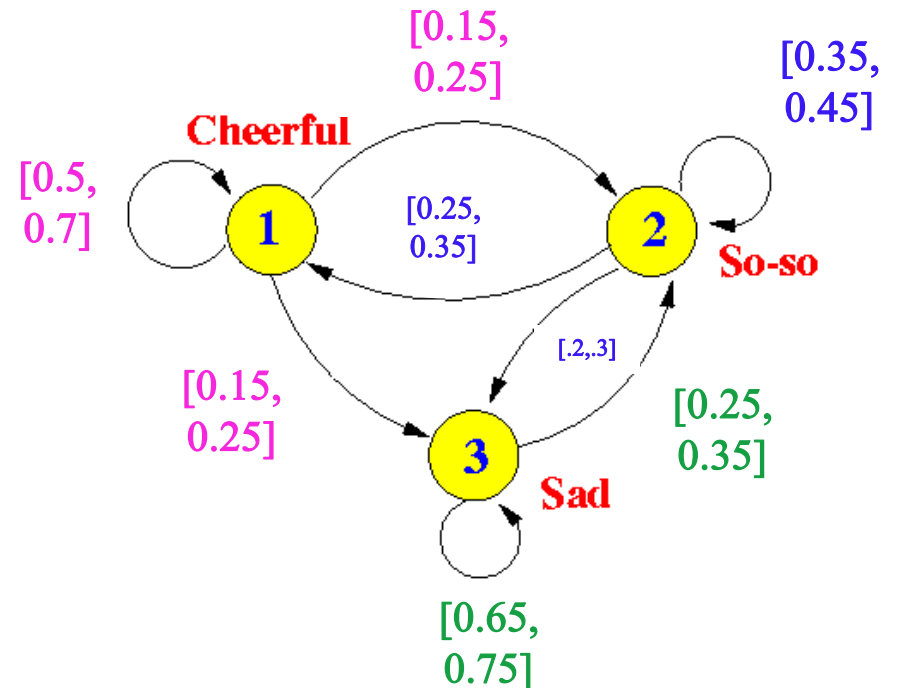
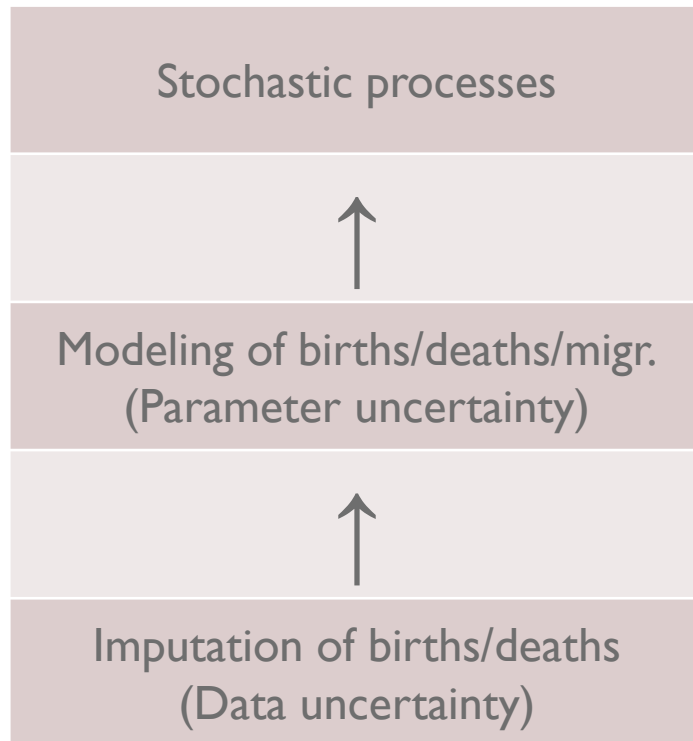




# Uncertainty

UNCERTAINTY refers to the quantifiable likelihood of outcomes other than the most likely one.

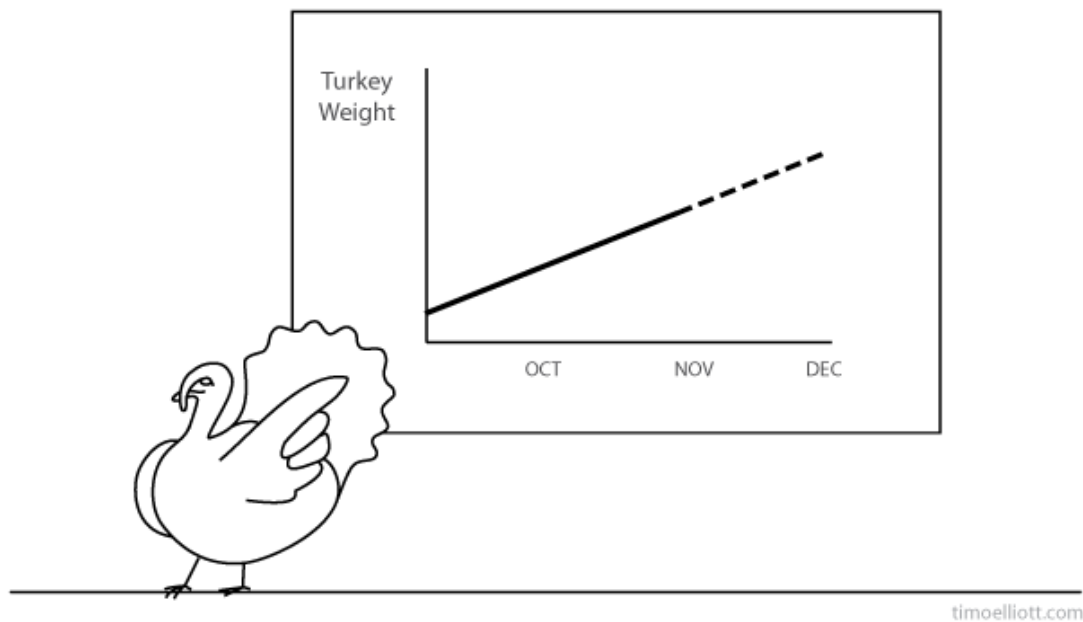
Uncertainty should be propagated from the following sources:





# Revisiting assumptions

## THANKSGIVING PREDICTIVE ANALYTICS



timoelliott.com

*"I see no reason why excellent growth shouldn't continue..."*

## Forecasting assumptions: relating the past and future

Models allow better assessment of past rates

- Accurate; complete; internally consistent; dynamic
- ... but does not tell the future.

Review past sources of error

- Too influenced by contemporary trends
- Lack of feedback mechanisms (i.e., agent behavior)

In first stage, incorporate three elements in review:

- (1) Historical trends
- (2) Demographic/sociological theory
- (3) Expert judgment

# Consultations and incorporating expert judgment

An approach to uncertainty: wisdom of crowds



NATURE

[MARCH 7, 1907]

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*Distribution of the estimates of the dressed weight of a particular living ox, made by 787 different persons.*

Degrees of the length of Array $0^{\circ}$ - $100^{\circ}$	Estimates in lbs.	Centiles		Excess of Observed over Normal
		Observed deviates from 1207 lbs.	Normal p.e = 37	
5	1074	-133	-90	+43
10	1109	-98	-70	+28
15	1126	-81	-57	+24
20	1148	-59	-46	+13
$q_1$ 25	1162	-45	-37	+8
30	1174	-33	-29	+4
35	1181	-26	-21	+5
40	1188	-19	-14	+5
45	1197	-10	-7	+3
$m$ 50	1207	0	0	0
55	1214	+7	+7	0
60	1219	+12	+14	-2
65	1225	+18	+21	-3
70	1230	+23	+29	-6
$q_3$ 75	1236	+29	+37	-8
80	1243	+36	+46	-10
85	1254	+47	+57	-10
90	1267	+52	+70	-18
95	1293	+86	+90	-4

$q_1, q_3$ , the first and third quartiles, stand at  $25^{\circ}$  and  $75^{\circ}$  respectively.  
 $m$ , the median or middlemost value, stands at  $50^{\circ}$ .  
The dressed weight proved to be 1193 lbs.

# Consultations and incorporating expert judgment

An approach to uncertainty: wisdom of crowds



NATURE

[MARCH 7, 1907]

*Distribution of the estimates of the dressed weight of a particular living ox, made by 787 different persons.*

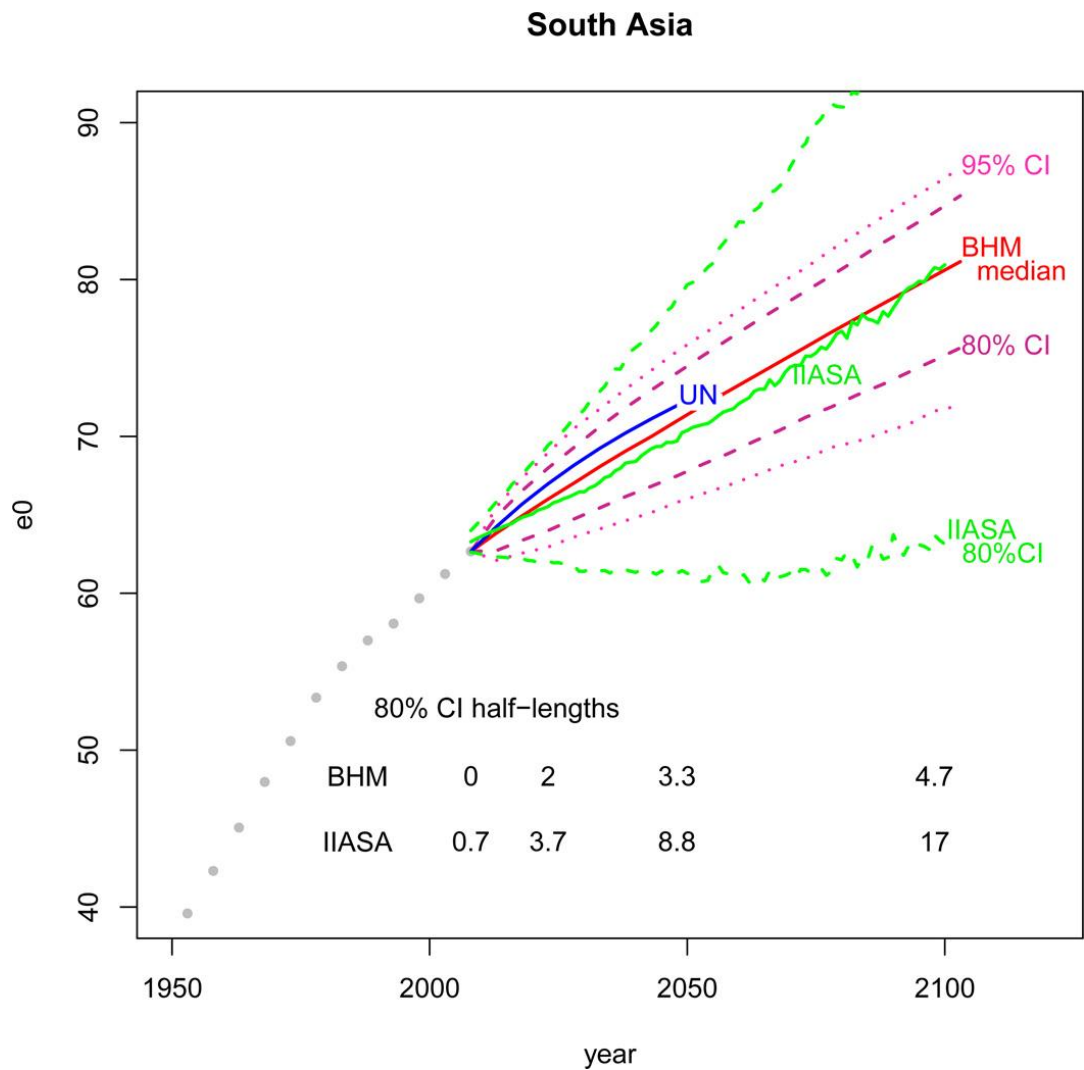
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5				
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25				
30				
35				
40				
45	1197	- 10	- 7	- 3
50	1207	0	0	0
55	1214	+ 7	+ 7	0
60	1210	+ 12	+ 14	+ 2
65	1230	+ 23	+ 29	- 6
70	1230	+ 23	+ 29	- 6
75	1230	+ 29	+ 37	- 8
80	1243	- 36	+ 40	- 10
85	1254	+ 47	+ 57	- 10
90	1267	+ 52	+ 70	- 18
95	1293	+ 86	+ 90	- 4



... including 'artificial crowds'

*q*<sub>1</sub>, *q*<sub>3</sub>, the first and third quartiles, stand at 25° and 75° respectively. *m*, the median or middlemost value, stands at 50°. The dressed weight proved to be 1193 lbs.

# Consultations and incorporating expert judgment



## Consultations and incorporating expert judgment

Collective wisdom of California experts in attendance